

Table of DTFT Pairs	
Time-Domain: $x[n]$	Frequency-Domain: $X(e^{j\hat{\omega}})$
$\delta[n]$	1
$\delta[n - n_0]$	$e^{-j\hat{\omega}n_0}$
$r_L[n] = u[n] - u[n - L]$	$\frac{\sin(\frac{1}{2}L\hat{\omega})}{\sin(\frac{1}{2}\hat{\omega})} e^{-j\hat{\omega}(L-1)/2}$
$r_L[n]e^{j\hat{\omega}_0n}$	$\frac{\sin(\frac{1}{2}L(\hat{\omega} - \hat{\omega}_0))}{\sin(\frac{1}{2}(\hat{\omega} - \hat{\omega}_0))} e^{-j(\hat{\omega} - \hat{\omega}_0)(L-1)/2}$
$\frac{\sin(\hat{\omega}_b n)}{\pi n}$	$u(\hat{\omega} + \hat{\omega}_b) - u(\hat{\omega} - \hat{\omega}_b) = \begin{cases} 1 &  \hat{\omega}  \leq \hat{\omega}_b \\ 0 & \hat{\omega}_b <  \hat{\omega}  \leq \pi \end{cases}$
$a^n u[n] \quad ( a  < 1)$	$\frac{1}{1 - ae^{-j\hat{\omega}}}$

Table of DTFT Properties		
Property Name	Time-Domain: $x[n]$	Frequency-Domain: $X(e^{j\hat{\omega}})$
Periodic in $\hat{\omega}$		$X(e^{j(\hat{\omega}+2\pi)}) = X(e^{j\hat{\omega}})$
Linearity	$ax_1[n] + bx_2[n]$	$aX_1(e^{j\hat{\omega}}) + bX_2(e^{j\hat{\omega}})$
Conjugate Symmetry	$x[n]$ is real	$X(e^{-j\hat{\omega}}) = X^*(e^{j\hat{\omega}})$
Conjugation	$x^*[n]$	$X^*(e^{-j\hat{\omega}})$
Time-Reversal	$x[-n]$	$X(e^{-j\hat{\omega}})$
Delay ( $n_d = \text{integer}$ )	$x[n - n_d]$	$e^{-j\hat{\omega}n_d} X(e^{j\hat{\omega}})$
Frequency Shift	$x[n]e^{j\hat{\omega}_0n}$	$X(e^{j(\hat{\omega} - \hat{\omega}_0)})$
Modulation	$x[n] \cos(\hat{\omega}_0n)$	$\frac{1}{2}X(e^{j(\hat{\omega} - \hat{\omega}_0)}) + \frac{1}{2}X(e^{j(\hat{\omega} + \hat{\omega}_0)})$
Convolution	$x[n] * h[n]$	$X(e^{j\hat{\omega}})H(e^{j\hat{\omega}})$
Autocorrelation	$x[-n] * x[n]$	$ X(e^{j\hat{\omega}}) ^2$
Parseval's Theorem	$\sum_{n=-\infty}^{\infty}  x[n] ^2$	$\frac{1}{2\pi} \int_{-\pi}^{\pi}  X(e^{j\hat{\omega}}) ^2 d\hat{\omega}$

<b>Table of Pairs for <math>N</math>-point DFT</b>	
<i>Time-Domain:</i> $x[n], \quad n = 0, 1, 2, \dots, N - 1$	<i>Frequency-Domain:</i> $X[k], \quad k = 0, 1, 2, \dots, N - 1$
If $x[n]$ is finite length, i.e., $x[n] \neq 0$ only when $n \in [0, N - 1]$ and the DTFT of $x[n]$ is $X(e^{j\hat{\omega}})$	$X[k] = X(e^{j\hat{\omega}}) \Big _{\hat{\omega}=2\pi k/N}$ (frequency sampling the DTFT)
$\delta[n]$	1
1	$N\delta[k]$
$\delta[n - n_0]$	$e^{-j(2\pi k/N)n_0}$
$e^{j(2\pi n/N)k_0}$	$N\delta[k - k_0]$ , when $k_0 \in [0, N - 1]$
$r_L[n] = u[n] - u[n - L]$ , when $L \leq N$	$\frac{\sin(\frac{1}{2}L(2\pi k/N))}{\sin(\frac{1}{2}(2\pi k/N))} e^{-j(2\pi k/N)(L-1)/2}$
$r_L[n]e^{j(2\pi k_0/N)n}$ , when $L \leq N$	$\frac{\sin(\frac{1}{2}L(2\pi(k - k_0)/N))}{\sin(\frac{1}{2}(2\pi(k - k_0)/N))} e^{-j(2\pi(k - k_0)/N)(L-1)/2}$
$\frac{\sin(\frac{1}{2}L(2\pi n/N))}{\sin(\frac{1}{2}(2\pi n/N))} e^{j(2\pi n/N)(L-1)/2}$	$N(u[k] - u[k - L])$ , when $L \leq N$

<b>Table of DFT Properties</b>		
<i>Property Name</i>	<i>Time-Domain:</i> $x[n]$	<i>Frequency-Domain:</i> $X[k]$
Periodic	$x[n] = x[n + N]$	$X[k] = X[k + N]$
Linearity	$ax_1[n] + bx_2[n]$	$aX_1[k] + bX_2[k]$
Conjugate Symmetry	$x[n]$ is real	$X[N - k] = X^*[k]$
Conjugation	$x^*[n]$	$X^*[N - k]$
Time-Reversal	$x[N - n]$	$X[N - k]$
Delay (PERIODIC)	$x[n - n_d]$	$e^{-j(2\pi k/N)n_d} X[k]$
Frequency Shift	$x[n]e^{j(2\pi k_0/N)n}$	$X[k - k_0]$
Modulation	$x[n] \cos((2\pi k_0/N)n)$	$\frac{1}{2}X[k - k_0] + \frac{1}{2}X[k + k_0]$
Convolution (PERIODIC)	$x[n] * h[n] = \sum_{m=0}^{N-1} h[m]x[n - m]$	$X[k]H[k]$
Parseval's Theorem	$\sum_{n=0}^{N-1}  x[n] ^2 = \frac{1}{N} \sum_{k=0}^{N-1}  X[k] ^2$	